

# Chapter 1

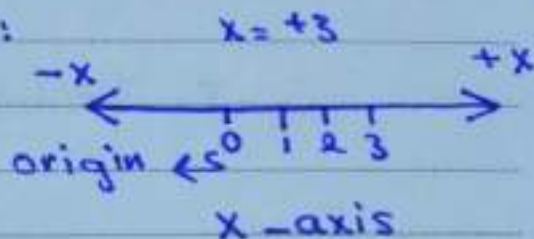
2020

No.

Medical physics :

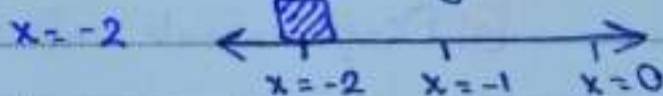
Ch. 1:

\* motion in one dimension:



\* position =  $x$

$\rightarrow x =$  How far from origin.

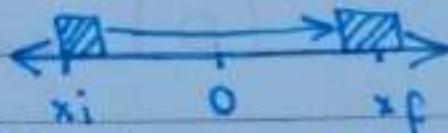


\* Displacement: الإزاحة  
vector  $\vec{\Delta x}$

$$\Delta x = x_f - x_i$$

$x_f \rightarrow$  نقطة الختام  
 $x_i \rightarrow$  نقطة البداية

$$\Delta x \begin{cases} \oplus \\ \ominus \end{cases} \quad - \text{ أو } + \text{ حسب اتجاه الحركة}$$

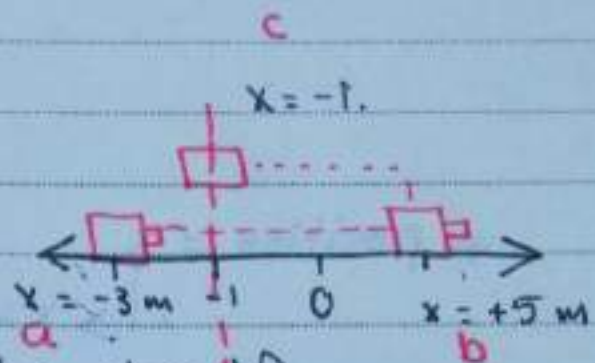


\* Distance: the length of the track

$\rightarrow$  scalar  $\rightarrow$  كمية

\*\* الإزاحة تعتمد على نقطتين : البداية والنهاية ، وليس المسار  
 الطريق المسلك .  
 بينما المسافة تعتمد على المسار .

Ex: In the figure, find:



a) Displacement of the object?

$$\Delta x = x_f - x_i = -1 + 3 = +2$$

b) Distance travelled by the object?

$$D = D_{a \rightarrow b} + D_{b \rightarrow c} \\ = 8 + 6 = 14 \text{ m}$$

$$[D] = \text{meter} = \text{m}$$

$$1 \text{ km} = 10^3 \text{ m}$$

$$1 \text{ Mm} = 10^6 \text{ m}$$

$$1 \text{ cm} = 10^{-2} \text{ m}$$

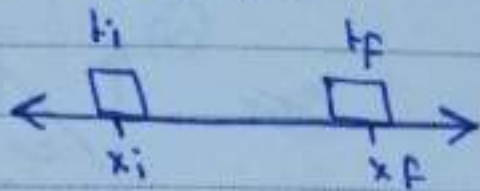
$$1 \text{ mm} = 10^{-3} \text{ m}$$

$$1 \text{ }\mu\text{m} = 10^{-6} \text{ m}$$

2

- Average velocity:  $\bar{v}$  أو  $v_{avg}$

\* Insta



$$v_{avg} = \frac{\Delta x}{\Delta t} = \frac{x_2(t_2) - x_1(t_1)}{t_2 - t_1} \Rightarrow \text{مع } x \text{ و } t \text{ في الاتجاهات}$$

$$[v] = m/s$$

if  $\Delta t \rightarrow 0$

$\therefore v_{avg} \rightarrow v_{inst}$  أو  $v$  في الاتجاه

$$v_{inst} = \frac{dx(t)}{dt}$$

\*  $\bar{v}$  أو  $v_{avg}$  ←  $\bar{v}$  أو  $v_{avg}$  مع  $\Delta t$  كبير +  $\Delta x$  كبير  
 \*  $v$  أو  $v_{inst}$  ←  $v$  أو  $v_{inst}$  مع  $\Delta t$  صغير +  $\Delta x$  صغير

- Average acceleration

$$a_{avg} = \frac{\Delta v}{\Delta t} = \frac{v_2(t_2) - v_1(t_1)}{t_2 - t_1}$$

$$[a] = m^2/s^2$$

$a_{avg} \rightarrow a_{inst}$  أو  $a$  في الاتجاه



$$x(t) \rightarrow v(t) \rightarrow a(t)$$

No.

c) The velocity of the car at  $t=2$  sec?

$$v_{\text{inst.}} \Big|_{t=2} = ?$$

$$6(t) + 2 \quad v_{\text{inst.}} = 6(2) + 2 = 14 \text{ m/s}$$

d) The acce. of the car for the period from  $t_1 = 1$  sec. to  $t_2 = 3$  sec.

$$a_{\text{avg}} = \frac{\Delta v}{\Delta t} = \frac{v_2(t_2) - v_1(t_1)}{t_2 - t_1}$$
$$= \frac{20 - 8}{2} = \frac{12}{2} = 6 \text{ m/s}^2$$

e) The acce. of the car at  $t=3$  sec.?

$$a(t=3 \text{ sec.}) = \frac{dv(t)}{dt} = 6 \text{ m/s}^2$$

\*\* Average Speed :  $\bar{v} = \frac{\text{total distance}}{\text{total time}}$

$$\text{average speed} = \frac{\text{travelled distance}}{\text{total time}}$$

$$= \frac{\text{المسافة الكلية}}{\text{الزمن الكلي}}$$

Ex: A car travelled 50 km with speed of 40 km/h then travelled another 30 km with speed of 20 km/h find its average speed.

Sol. Ave. speed =  $\frac{\text{distance}}{\text{time}}$

① حسب الزمن للسرعة / المسافة الأوتى و التايق  
لإيجاد الزمن الكلى .

$$\text{distance} = 50 + 30 = 80 \text{ km/h}$$

$$t_{\text{tot.}} = t_1 + t_2$$

$$T_1 = \frac{S}{d} = \frac{50}{40}$$

$$T_2 = \frac{30}{20}$$

$$T_{\text{tot.}} = 2.75 \text{ h}$$

$$\text{Ave. speed} = \frac{80}{\frac{11}{4}} = \frac{320}{11} \approx 29.1 \text{ km/h} = 8.08 \text{ m/s}$$

$$1 \text{ km/h} \rightarrow \frac{1000}{3600} \text{ m/s}$$

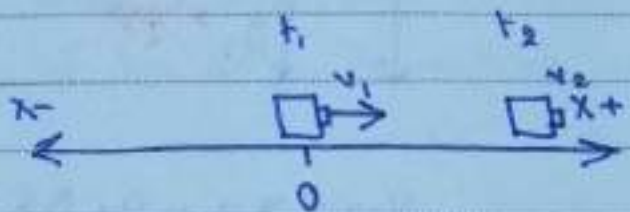
\* حتم يحل السؤال على مثال رسم بياني  
\* حتم يحل سرعة و زمن و يوجد المسافة \*

## 1.5 Motion in a straight line with constant acceleration : الحركة في مستقيم مع تسارع ثابت

$a$  is constant.

\* التسارع ثابت

\* A long  $x$ -axis :



$$v_2 = v_1 + a \Delta t \quad \text{--- (1)}$$

$$v_2 \Delta t + \frac{1}{2} a \Delta t^2 = x_2 - x_1$$

$$x_2 = x_1 + v_1 \Delta t + \frac{1}{2} a \Delta t^2 \quad \text{--- (2)}$$

$$v_2^2 = v_1^2 + 2a \Delta x \quad \text{--- (3)}$$

$$v_2^2 - v_1^2 = 2a(x_2 - x_1)$$

(-) decce.  $\rightarrow$  يتباطأ  $\rightarrow$   $x \ominus$  باتجاه

$a <$

(+) acce.  $\rightarrow$  تسارع  $\rightarrow$   $x \oplus$  باتجاه

باتجاه +

Ex: A bus starts its motion from rest towards  $+x$  axis

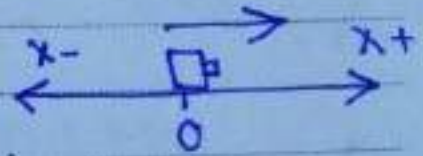
السرعة  $v_1 = 0$

إذا لم تسر  $t_1 = 0$

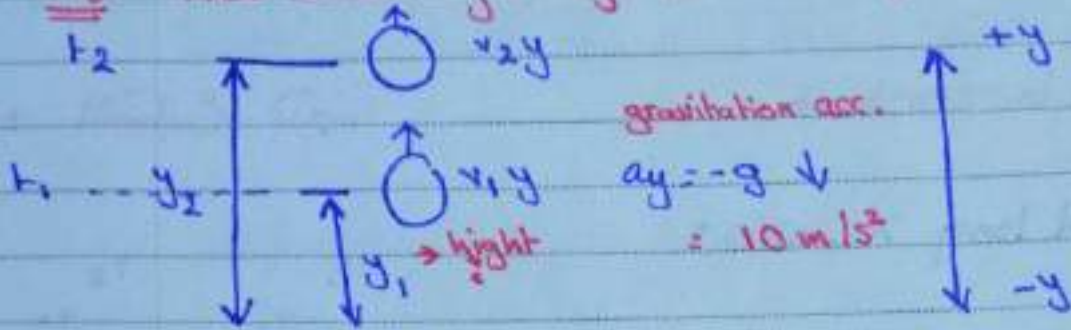
Find its velocity after 15 sec. if it acc. =  $4 \text{ m/s}^2$

$$v_{2x} = v_{1x} + a_x \Delta t$$

$$= 0 + 4(15) = 60 \text{ m/s.}$$



1.6 Free-Falling objects: السقوط الحر



①

$$v_{2y} = v_{1y} + a_y \Delta t \quad \text{--- (1)}$$

$$y_2 = y_1 + v_{1y} \cdot \Delta t + \frac{1}{2} a_y (\Delta t)^2 \quad \text{--- (2)}$$

$$v_{2y}^2 = v_{1y}^2 + 2 a_y \Delta y \quad \text{--- (3)}$$

②

$$v_{2y} = v_{1y} + (-g) \Delta t$$

$$y_2 = y_1 + v_{1y} \cdot \Delta t + \frac{1}{2} (-g) (\Delta t)^2$$

$$v_{2y}^2 = v_{1y}^2 + 2 (-g) \Delta y$$

← السقوط الحر لا يحدث بداية الحركة من السكون  
 ← الأجسام المساقطة سقوطاً حراً: هي الأجسام المتحركة عند تأثير مجال الجاذبية الأرضية ولا تدفع مطلقاً الأجسام التي تبدأ الحركة من السكون.  
 ← يمكن أن يكون لها سرعة ابتدائية  $\neq$  صفر.

② هذه القوانين تطبق مع ما يلي:  $y$   
 + بالنسبة للارتفاع  $\leftarrow$  فوق سطح الأرض (+) ، عند سطح الأرض (-)  
 أي أن نقطة الميز (الرجح) هي سطح الأرض.





b. The max. high that the ball can reach? with respect to ground

→ Elimination is

$$v_{1y} = 4 \text{ m/s} \quad v_{2y} = 0 \text{ m/s}$$

$$y_1 = 20 \text{ m} \quad y_2 = ?!$$

$$v_{2y}^2 = v_{1y}^2 - 20 \Delta y$$

$$0 = 16 - 20 \Delta y \quad \frac{20(y_2 - 20)}{20} = \frac{16}{20}$$

$$y_2 - \cancel{20} + \cancel{20} = \frac{16}{20} + 20 = 20.8 \text{ m.}$$

$$v_{\text{avg}} = \frac{x_2(t_2) - x_1(t_1)}{t_2 - t_1}$$

$$v_{\text{inst.}} = \frac{dx(t)}{dt}$$

$$a_{\text{avg}} = \frac{\Delta v}{\Delta t} = \frac{v_2(t_2) - v_1(t_1)}{t_2 - t_1}$$

avg. speed =

$$\frac{\text{travelled distance}}{\text{total time}}$$

$$v_{2x} = v_{1x} + a_x \Delta t$$

$$v_{2x}^2 = v_{1x}^2 + 2a_x \Delta x$$

$$x_{2x} = v_{1x} \Delta t + \frac{1}{2} a_x \Delta t^2$$

$$v_{y2} = v_{y1} - 10 \Delta t$$

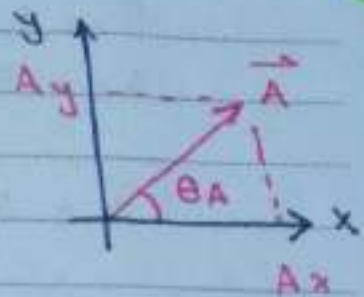
$$y_2 = y_1 + v_{y1} \Delta t - 5 \Delta t^2$$

$$v_{y2}^2 = v_{y1}^2 - 20 \Delta y$$

# Chapter 2

Ch 3 vectors :

$\vec{A}$   $\equiv$  vector A  
 $\equiv$  has magnitude



$|\vec{A}|$  and direction  $\theta_A$

$\vec{A}$  has two components :  $A_x = x$ -Component  
 $A_y = y$ -Component.

$$\left. \begin{aligned} A_x &= |\vec{A}| \cos \theta_A \\ A_y &= |\vec{A}| \sin \theta_A \end{aligned} \right\} \theta_A \equiv \text{measure with respect to } +x$$

• احسب طول المتجه  $\vec{A}$

From (1) and (2) we can obtain :

$$|\vec{A}| = \sqrt{(A_x)^2 + (A_y)^2} \quad (3)$$

$$\theta_A = \tan^{-1} \frac{A_y}{A_x} \quad \downarrow \text{inverse} \quad (4)$$

## 3.2 Unit vectors ، متجهات الوحدة

هي متجهات لها مقدار قيمته وحدة واحدة

$$\begin{aligned} \hat{i} & \hat{j} & \hat{k} \\ |\hat{i}| & |\hat{j}| & |\hat{k}| = 1 \\ \text{direction } +x & +y & +z \end{aligned}$$

Ex: If  $\vec{A}$  is a vector which has  $A_x = +3$ ,  $A_y = -4$ ,  $A_z = +5$ . write  $\vec{A}$  using the unit vector.

$$\begin{aligned} \vec{A} &= A_x \hat{i} + A_y \hat{j} + A_z \hat{k} \\ &= 3\hat{i} + (-4)\hat{j} + 5\hat{k} \\ &= 3\hat{i} - 4\hat{j} + 5\hat{k} \end{aligned}$$

### 2.3 Resultant vector:

if  $\vec{A}$ ,  $\vec{B}$ ,  $\vec{C}$ , etc. are vectors, then

$R$   $\equiv$  the resultant vector can be calculated as follows.

① Finding the x component of all vector

$$A_x = |\vec{A}| \cos \theta_{Ax}$$

يجب أن تكون الزاوية بالنسبة لـ x+

$$B_x = |\vec{B}| \cos \theta_{Bx}$$

$$C_x = |\vec{C}| \cos \theta_{Cx}$$

② Finding the y component of all vector

$$A_y = |\vec{A}| \sin \theta_{Ay}$$

$$B_y = |\vec{B}| \sin \theta_{By}$$

$$C_y = |\vec{C}| \sin \theta_{Cy}$$

2/

\* يجب التأكيد على أنه كل الزوايا لخطاف المتجهان يجب أن تقاس  
من / بالنسبة لمحور  $x^+$  على عقارب الساعة.

\* عند استخدام الآلة الحاسبة يجب التأكيد من أن تلك  
الزاوية مقاسة بالدرجات لأن الآلة الحاسبة لها  $\frac{\pi}{180}$  لتحويل  
حساب الزاوية.

③ Finding the  $R_x$  -  $x$  - component of the result  
that vector, by adding the  $x$  - components  
of all vectors.

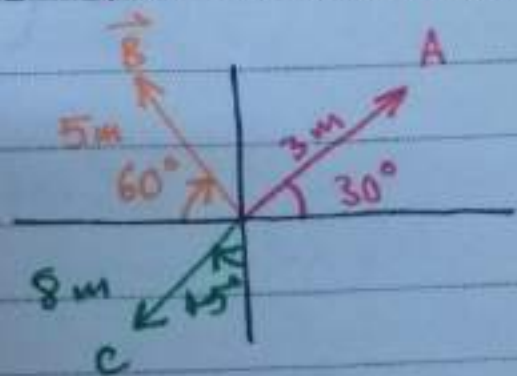
$$R_x = A_x + B_x + C_x + \dots$$

④  $R_y$  will be:  $R_y = A_y + B_y + C_y$ .

⑤ the magnitude of  $\vec{R}$  will be  $|\vec{R}| = \sqrt{(R_x)^2 + (R_y)^2}$

⑥ the direction of  $R$  will be  $\theta_R = \tan^{-1}\left(\frac{R_y}{R_x}\right)$

Ex: In the figure  $\vec{A}$ ,  $\vec{B}$ ,  $\vec{C}$  are vectors. Find  
the result vector.



$$|\vec{A}| = 3 \text{ m}, \theta_A = 30^\circ$$

$$|\vec{B}| = 5 \text{ m}, \theta_B = 120^\circ$$

$$|\vec{C}| = 8 \text{ m}, \theta_C = 225^\circ$$

$$A_x = 3 \cos(30) = 2.59 \quad A_y = 3 \sin(30) = 1.5$$

$$B_x = 5 \cos(120) = -2.5 \quad B_y = 5 \sin(120) = 4.33$$

$$C_x = 8 \cos(225) = -5.65 \quad C_y = 8 \sin(225) = -5.65$$

$$R_x = -5.55 \text{ m} \quad |\vec{R}| = \sqrt{(R_x)^2 + (R_y)^2}$$

$$R_y = 0.17 \text{ m} \quad = 5.55$$

$$\theta_R = -1.75^\circ$$



\*\* Finding the resultant by unit vectors!

$$\text{If } \vec{A} = A_x \hat{i} + A_y \hat{j} + \cancel{A_z \hat{k}} \quad \vec{B} = B_x \hat{i} + B_y \hat{j}$$

$$\vec{R} = R_x \hat{i} + R_y \hat{j}$$

$$|\vec{R}| = \sqrt{(R_x \hat{i})^2 + (R_y \hat{j})^2}$$

$$\theta = \tan^{-1} \left( \frac{R_y \hat{j}}{R_x \hat{i}} \right)$$

## \* \* Vector product :-

### 1. Dot product (scalar product)

Case 1: If  $\vec{A}$  and  $\vec{B}$  are vectors, then

$$\vec{A} \cdot \vec{B} = |\vec{A}| |\vec{B}| \cos \theta_{AB}$$

مقدار ضرب مقدار



$$\text{Case 2: If } \left. \begin{array}{l} \vec{A} = A_x \hat{i} + A_y \hat{j} \\ \vec{B} = B_x \hat{i} + B_y \hat{j} \end{array} \right\} \begin{array}{l} \vec{A} \cdot \vec{B} = CA \cdot CB \\ = (A_x \cdot B_x) + (A_y \cdot B_y) \end{array}$$

Ex: If  $\vec{A} = 3\hat{i} - 2\hat{j} + 4\hat{k}$  Find the angle bet.  $\vec{A}, \vec{B}$   
 $\vec{B} = 6\hat{i} + \hat{j} - 5\hat{k}$

$$\vec{A} \cdot \vec{B} = |\vec{A}| |\vec{B}| \cos \theta_{AB} \rightarrow \cos \theta_{AB} = \frac{\vec{A} \cdot \vec{B}}{|\vec{A}| |\vec{B}|} \quad \text{--- (1)}$$

$$|\vec{A}| = \sqrt{A_x^2 + A_y^2 + A_z^2} = \sqrt{3^2 + (-2)^2 + 4^2} = 5.3 \quad \text{--- (2)}$$

$$|\vec{B}| = \sqrt{B_x^2 + B_y^2 + B_z^2} = \sqrt{6^2 + 1^2 + (-5)^2} = 7.8 \quad \text{--- (3)}$$

$$\begin{aligned} \vec{A} \cdot \vec{B} &= A_x \cdot B_x + A_y \cdot B_y + A_z \cdot B_z \\ &= -4 \quad \text{--- (4)} \end{aligned}$$

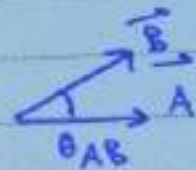
2, 3, 4 in (1) we get  $\cos \theta_{AB} = \frac{-4}{5.3 (7.8)}$

$$\theta_{AB} = 95.5^\circ$$

5 //

\* Cross product: if  $\vec{A}$  and  $\vec{B}$  are vectors,  
then

$$|\vec{A} \times \vec{B}| = |\vec{A}| |\vec{B}| \sin \theta_{AB}$$

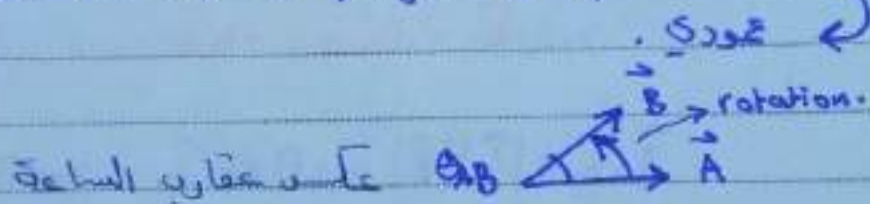


دائري من اليمين الى اليسار ←

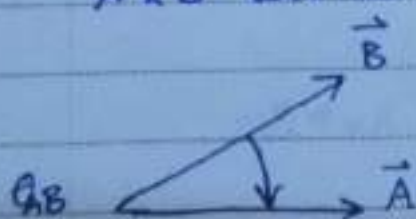
$$\vec{A} \times \vec{B} \Rightarrow \vec{A} \rightarrow \vec{B} \quad \vec{B} \rightarrow \vec{A}$$

نتيجة: This means that the direction can be found  
as follows:

- ① If the rotation from  $\vec{A}$  to  $\vec{B}$  is counter clockwise as shown in the figure then the direction of  $\vec{A} \times \vec{B}$  will be out of page. (perpendicular)



- ② If the rotation from  $\vec{A}$  to  $\vec{B}$  is clockwise as shown in the figure then the direction of  $\vec{A} \times \vec{B}$  will be inside of page (x)





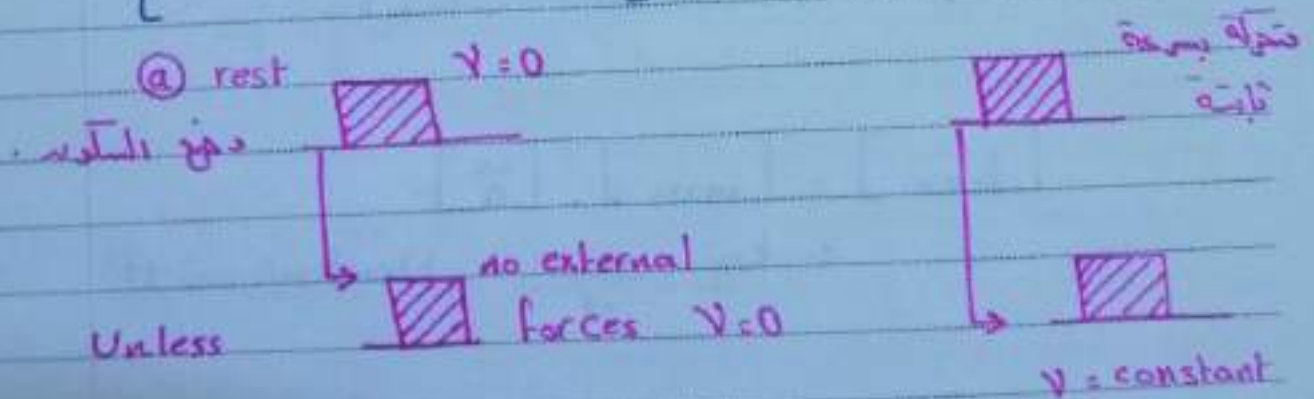
# Chapter 3

## Ch 4. Newton's Laws : "Dynamics"

\* Newton's first law  $\equiv$  [law of inertia]  
discussing the static situation of objects and  
it state's that ~~for~~

The object @ rest / moving with constant / uniform  
velocity remains @ rest or moving with constant /  
Uniform velocity Unless an external forces act(s)  
on the object ~~at rest~~ and leads to change  
it's static situation.

\* \* [ mass  $\xrightarrow{\text{why?}}$  Inertia ]



$|\vec{a}| = \text{Zero}$

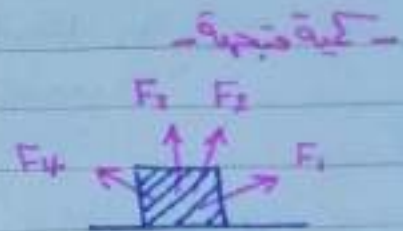
الحالة = سرعة في اتجاه واحد فقط

$v = \text{constant} = \text{uniform motion.}$

تغيره ببطء

exert  $\rightarrow$   $\vec{F}$

\* Newton second law  
Force concept law



$$\vec{F} \text{ resultant} = \sum \vec{F} \propto \vec{a}$$

$\propto$ : direct proportion

تساوي مباشر

$$\left[ \sum \vec{F} = \vec{F} \text{ resultant} = m \cdot \vec{a} \right] :$$

الاتجاه الحركي

①  $\vec{F} \text{ resultant} \uparrow \uparrow$  motion  $\vec{a} \rightarrow \oplus$  acceleration

direction: تسارع

تساوي

②  $\vec{F} \text{ resultant} \downarrow \downarrow$  motion  $\vec{a} \rightarrow \ominus$  acceleration.

↳ Ex: Friction force قوة الاحتكاك

$$[\text{force}] = [\text{mass}] \cdot [\vec{a}]$$

$$= \text{kg} \cdot \frac{\text{m}}{\text{s}^2} = \text{Newton} = \text{N}$$

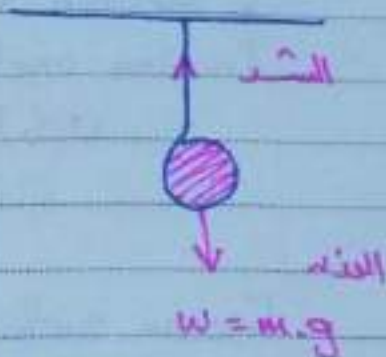
$$[F] = \frac{\text{g} \cdot \text{cm}}{\text{s}^2} = \text{dyne}$$

\* Forces:

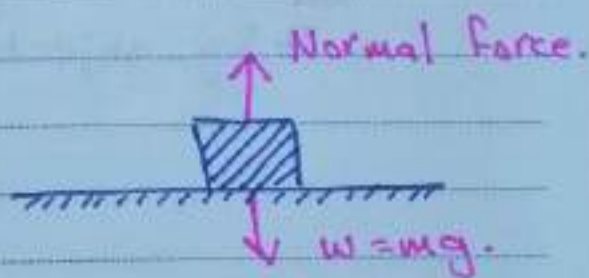
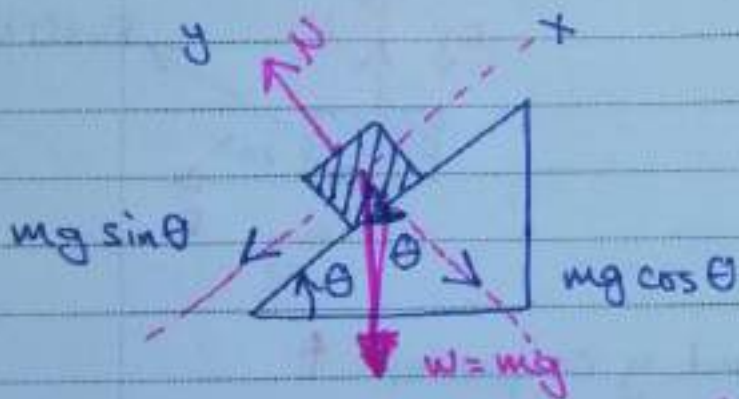
① weight.

② Tension =  $T$  قوة الشد

③ Normal force =  $\vec{N}$  القوة العمودية



$\vec{N} \perp$  surface

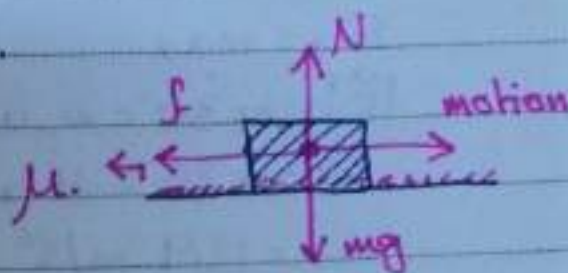


سطح مائل

④ Friction قوة الاحتكاك

• اتجاهها عكس اتجاه الحركة.

smooth no friction.      rough Friction.



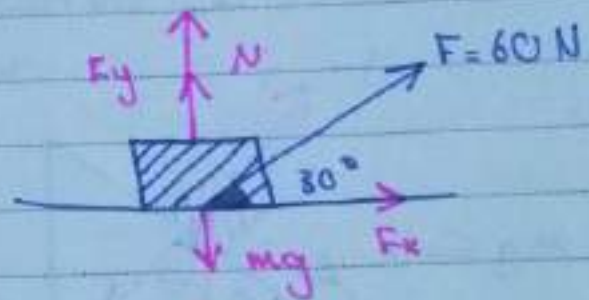
\* For the sur tough surfaces, there is friction coefficient :

$$0 \leq \mu \leq 1$$

smooth surface  $\Leftrightarrow \mu = 0$  line

$$\text{Friction surface} = |\vec{f}| = \mu \cdot |\vec{N}|$$

Ex : In the figuer, Find the acceleration of 4 kg object?



① Find the x and y component

② Drawing free-body Diagram.

③ Applying Newton second law.

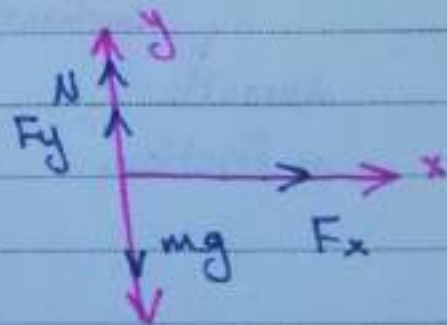
● x-axis :

$$\Sigma F_x = m a_x$$

$$|\vec{F}| \cos 30 = m \cdot a_x$$

$$60 \cos 30 = 4 a_x$$

$$a_x = 12.9 \text{ m/s}^2$$

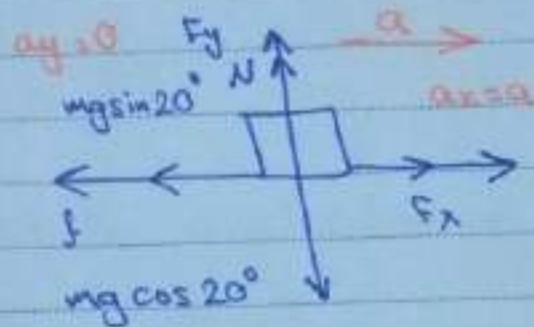
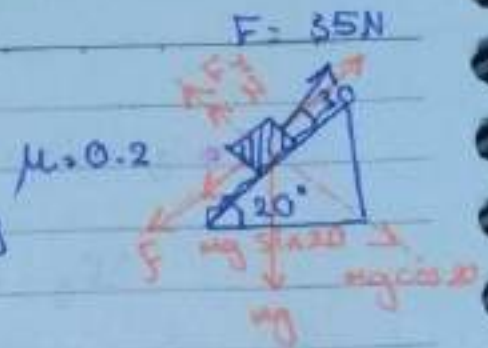


• y-axis:

$$\sum F_y = may \Rightarrow 0 = \text{النسبة}$$

• لا يوجد حركة على المحاور الأخرى.

Ex: In the figure, find the acceleration of the 6 kg object?



x-axis:

$$\Sigma F_x = ma$$

$$F_x - f - mg \sin 20$$

$$35 \cos 30 - \mu \cdot N - mg \sin 20 = ma$$

$$35 \cdot 0.86 - 0.2N - 6 \times 10 (0.34) = 6a$$

$$30.1 - 0.2N - 20.4 = 6a$$

$$9.7 - 0.2N = 6a \quad \text{--- (a)}$$

y-axis:

$$\Sigma F_y = may$$

$$F_y + N - mg \cos 20 = m(0)$$

$$F_y + N - mg \cos 20 = 0$$

$$|F| \sin 30 + N - mg \cos 20 = 0$$

$$35 \cdot \frac{1}{2} + N - 6 \times 10 \times 0.9 = 0$$

$$17.5 + N - 54 = 0$$

$$N = 36.5$$

$$6a = 9.7 - 0.2N$$

$$6a = 9.7 - 0.2(36.5)$$

$$\frac{6a}{6} = 9.7 - 7.3 = \frac{2.4}{6}$$

$$a = 0.4 \text{ m/s}^2$$

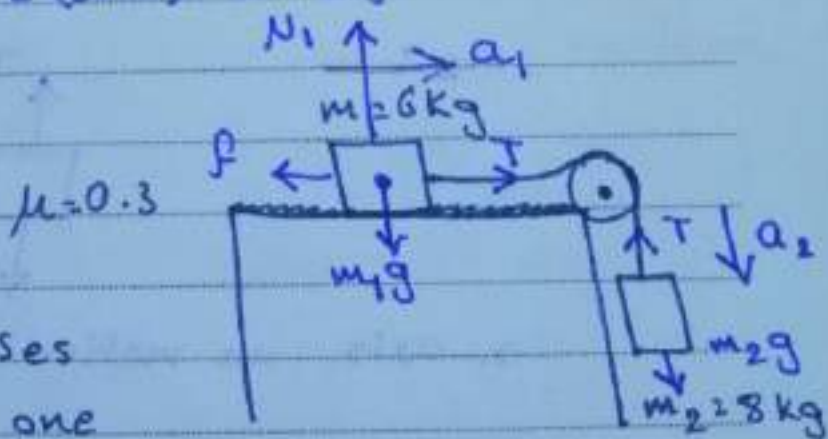
(b)  $f = ?$

$$|f| = \mu \cdot N = 0.2(36.5) = 7.3$$

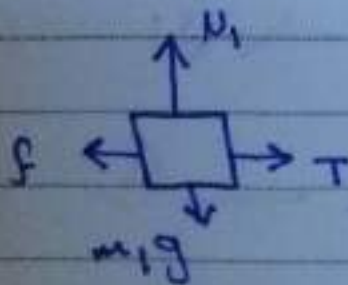
Ex:

In the figure, a system of two masses  $m_1$  and  $m_2$  which are

connected by a string over a frictionless pulley. Find the acceleration of the system?



$m_1$  :-



x-axis:

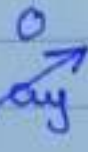
$$\Sigma F_x = m_1 a_x$$

$$T - F = m_1 a_1$$

$$T - \mu N_1 = m_1 a_1$$

$$T - 0.3 N_1 = 6 a_1 \quad \text{--- (1)}$$

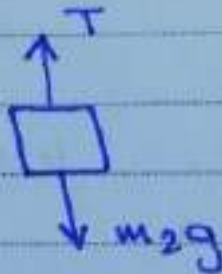
y-axis:

$$\Sigma F_y = m_1 a_y$$


$$N_1 = m_1 g$$

$$N_1 = 60 \text{ N} \quad \text{--- (2)}$$

$m_2$ :



x-axis no motion

y-axis:  $T - m_2 g = m_2 a_2$

$$T - m_2 g = 8 a_2 \quad \text{--- (3)}$$

$$T = 80 + 8 a_2 \quad \text{--- (3)}$$



$$T - 0.3(60) = 6a,$$

$$80 + 8a - 18 = 6a$$

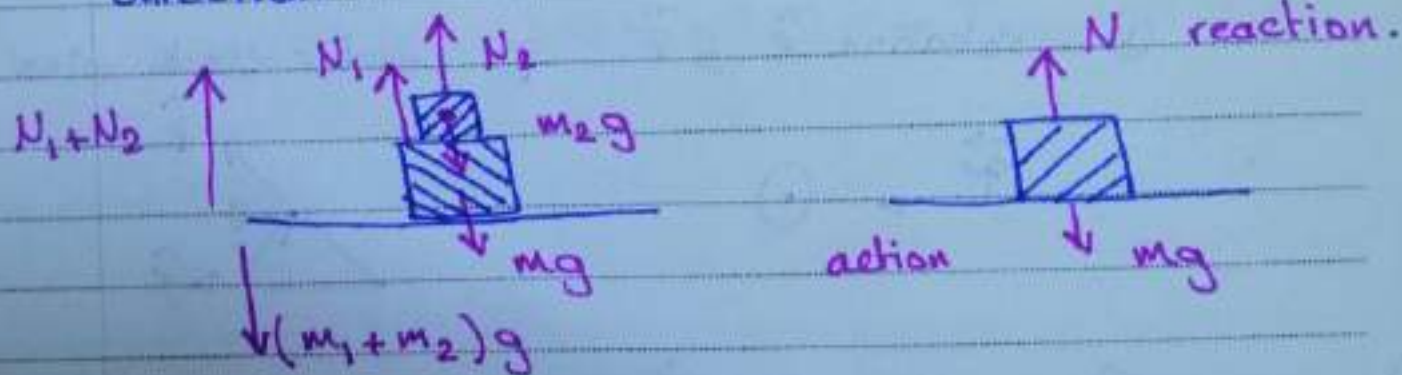
$$(8 - 6)a = 18 - 80$$

$$\frac{2a}{2} = \frac{-62}{2}$$

$$a = -31 \text{ m/s}^2$$

● Newton's Third law: (Action reaction law)

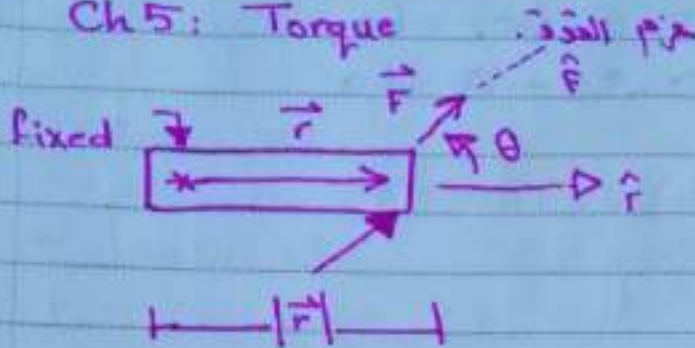
Each action has a reaction, in which both are equal in magnitude and opposite in direction.



# Chapter 4

No.

Ch 5: Torque



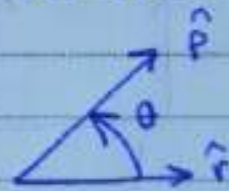
$$\vec{\tau} = \vec{r} \times \vec{F}$$

$$|\tau| = |\vec{r}| |\vec{F}| \sin \theta$$

\* Direction:

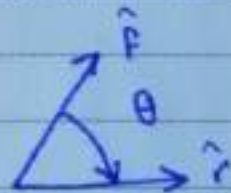
① rotation  $\hat{r} \rightarrow \hat{F} \Rightarrow$  counter clock wise

$$\vec{\tau} \rightarrow \odot$$



② rotation  $\hat{r} \rightarrow \hat{F} \Rightarrow$  clock wise

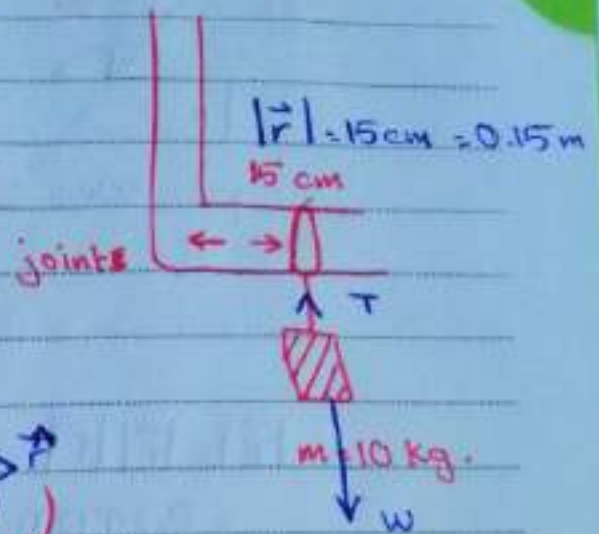
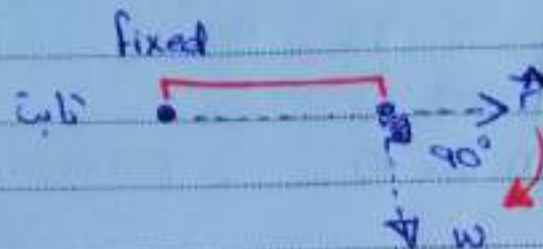
$$\vec{\tau} \rightarrow \otimes$$



$$[\vec{\tau}] = [r][F] = \text{N.m}$$

Ex: In the figure find the torque done by the 10 kg mass.

Sol.



$$|\vec{\tau}| = |\vec{r}| |\vec{F}| \sin \theta$$

(1)

$$= 10 (10) = 100 \text{ N} \times 0.15 \times \sin 90^\circ = 15 \text{ N.m}$$

Direction: clock wise

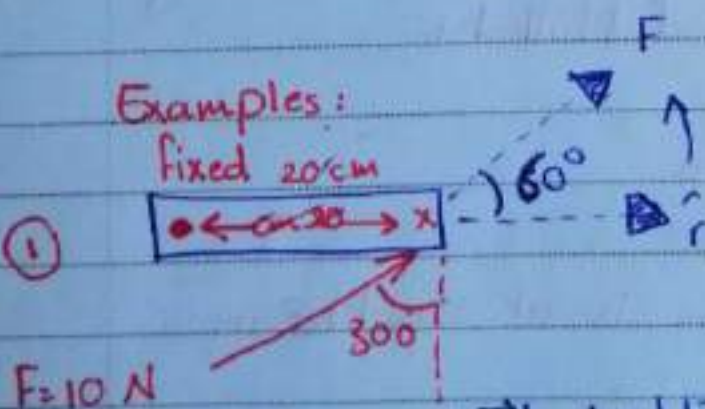
$$\vec{\tau} = 15 \text{ N.m} (\otimes)$$

$$(\sin \theta) F \perp r$$

Examples:

fixed 20 cm

(1)

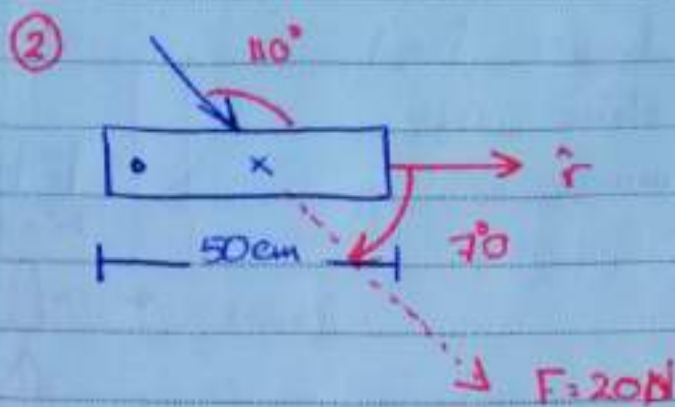


$$F = 10 \text{ N}$$

$$\text{Find } \vec{\tau} ? \quad |\vec{\tau}| = |\vec{r}| |\vec{F}| \sin \theta$$

(1)

$$= 1.72 \text{ N.m}$$



$$|\vec{\tau}| = |\vec{r}| |F| \sin\theta$$

$$= 0.25 (20) \sin 70$$

### Ex-2: Static and Equilibrium:

Conditions: ① the forces must be at equilibrium

$$\sum F = 0$$

$$\text{② } \sum \tau = 0$$

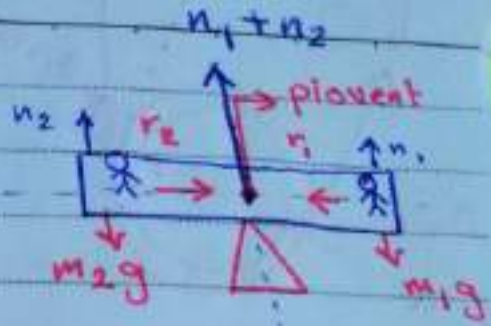
\* Equilibrium exists if the following conditions are fulfilled:

$$\text{① } \sum \vec{F} = \text{Zero}$$

$$\text{② } \sum \vec{\tau} = \text{Zero}$$

Then the system is at equilibrium

دو جسم متساويين الكتلة  
 إذا كانت المسافات متساوية  
 عن نقطة الاتزان

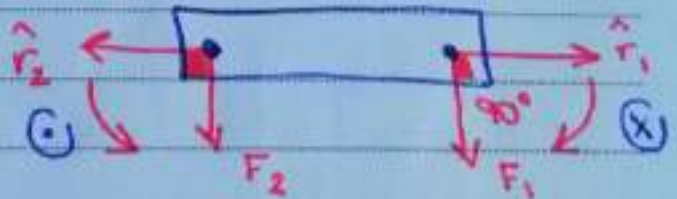


إذا كانت المسافات غير متساوية  
 عن نقطة الاتزان

Ex:

①  $\Sigma F = 0$

②  $\Sigma \tau = 0$



$\tau_1 + \tau_2 = 0 \checkmark$

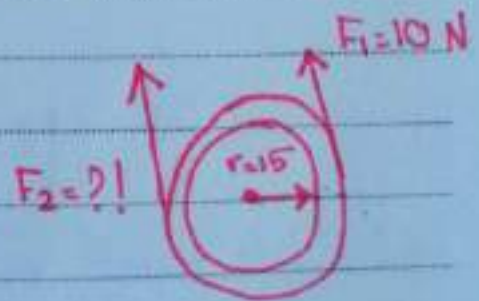
$r_1 F_1 \sin \theta_1 = r_2 F_2 \sin \theta_2$

$|\tau_1| = |\tau_2|$

~~$r_1 m_1 g \sin 90 = r_2 m_2 g \sin 90$~~

$r_1 m_1 = r_2 m_2$

Ex: Find  $F_2$  for equilibrium?

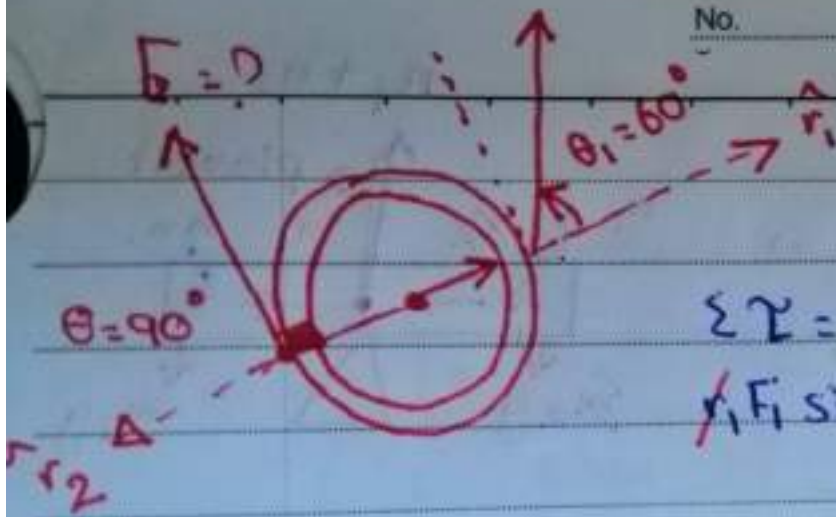


$F_2 = 10 \text{ N}$

تساوي القوتان لأن المسافات متساوية

$$F_1 = 20 \text{ N}$$

No. \_\_\_\_\_



∴ حالة ثانية

$$\sum \tau = 0$$

$$\cancel{r_1} F_1 \sin 60 = 1$$
$$= \cancel{r_2} F_2 \sin 90$$

$$F_1 \sin 60 = F_2$$

$$F_2 = 20 \times 0.86 = 17.2 \text{ N}$$

5

# Chapter 5

Ch 6: work and energy:-

work: form of energy (gained) (w)  
lost

\* work done by force/forces acting on an object leading to displace the object from place to another one ~~be~~ can be ~~calc~~ calculated as follows:

$$W = \vec{F} \cdot \Delta \vec{r} \quad w = |\vec{F}_{net}| \cdot |\Delta \vec{r}| \cdot \cos \theta$$

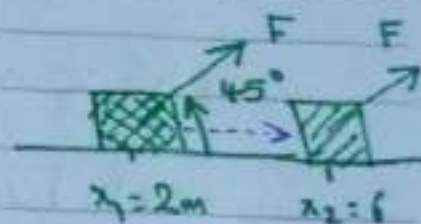
✱ If  $\vec{F} = F_x \hat{i} + F_y \hat{j} + F_z \hat{k}$  and the object is moved from  $\vec{r}_1 = r_{1x} \hat{i} + r_{1y} \hat{j} + r_{1z} \hat{k}$  to  $\vec{r}_2 = r_{2x} \hat{i} + r_{2y} \hat{j} + r_{2z} \hat{k}$  then the work will be

$$W = \vec{F} \cdot \Delta \vec{r} = (F_x \hat{i} + F_y \hat{j} + F_z \hat{k}) \cdot (\Delta x \hat{i} + \Delta y \hat{j} + \Delta z \hat{k}) \\ = (F_x \Delta x) + (F_y \Delta y) + (F_z \Delta z)$$

$$[W] = [F][\Delta r] = N \cdot m = J.$$

العمل = القوة × المسافة في اتجاه القوة  
-  $\vec{r}_1$  +  $\vec{r}_2$  المسافة في اتجاه القوة  
-  $\vec{r}_1$  المسافة في اتجاه القوة

Ex 1 In the figure find the work done by  $\vec{F}$



$$\begin{aligned} W &= |\vec{F}| |\Delta r| \cos \theta \\ &= 20 \times (6-2) \cos 45^\circ \\ &= 20 (4) \cos 45 = 56.5 \text{ J} \end{aligned}$$

Ex 2: If the following forces are acting on 6 kg object. The object is therefore moved from point  $r_1 = (2, 6, -1)$  to point  $r_2 (1, -1, 5)$ . Find the work done on the object?

$$F_1 = 6\hat{i} + 8\hat{j} + 3\hat{k}$$

$$F_2 = 2\hat{i} + 6\hat{j}$$

$$\begin{aligned} \vec{F}_{\text{net}} &= \vec{F}_1 + \vec{F}_2 \\ &= (6\hat{i} + 8\hat{j} + 3\hat{k}) + (2\hat{i} + 6\hat{j} + 0\hat{k}) \\ &= 4\hat{i} + 14\hat{j} - 3\hat{k} \end{aligned}$$

$$\begin{aligned} \Delta \vec{r} &= r_2 - r_1 \\ &= (1\hat{i} - 1\hat{j} + 5\hat{k}) - (2\hat{i} + 6\hat{j} - 1\hat{k}) \\ &= 1\hat{i} - 1\hat{j} + 5\hat{k} - 2\hat{i} - 6\hat{j} + 1\hat{k} \\ &= -\hat{i} - 7\hat{j} + 6\hat{k} \end{aligned}$$

$$\begin{aligned} W &= \vec{F}_{\text{net}} \cdot \Delta \vec{r} = (4\hat{i} + 14\hat{j} - 3\hat{k}) \cdot (-\hat{i} - 7\hat{j} + 6\hat{k}) \\ &= -4\hat{i}\hat{i} - 98\hat{j}\hat{j} - 18\hat{k}\hat{k} \\ &= -120 \text{ J} \Rightarrow \text{lost work} \end{aligned}$$

2



حالات الشغل :

①  $w \rightarrow \text{max} \rightarrow \theta = \text{Zero}$

②  $w \rightarrow \text{Zero} \rightarrow \theta = 90^\circ$

③  $w \rightarrow \text{min} \rightarrow \theta = 180^\circ$

$w$  ———  $\oplus \rightarrow \text{gained}$   
          —  $\ominus \rightarrow \text{lost.}$

2)  $\cos 45^\circ$

+)  $\cos 45$

Ex 2: If the following  
on 6 kg object. The

$6\hat{i} + 8\hat{j} + 3\hat{k}$

- Potential Energy  $\equiv U \rightarrow J$   
 $\hookrightarrow$  gravitational P.E

أي جسم له ارتفاع وكتلة له طاقة مخزنة.

$$U = m \cdot g \cdot y$$

$\rightarrow$  height.



- العلاقة بين الشغل والطاقة  $\leftarrow$  الطاقة

$$W = -\Delta U$$

\* work by object  $\rightarrow$  lose some of U  
 work done on the object  $\rightarrow$  gained some of U

- Kinetic Energy  $\equiv K \rightarrow J$ .

$$K = \frac{1}{2} m v^2 \rightarrow \text{velocity.}$$

$\downarrow$   
mass

- العلاقة بين الشغل والطاقة  $\leftarrow$  الشغل

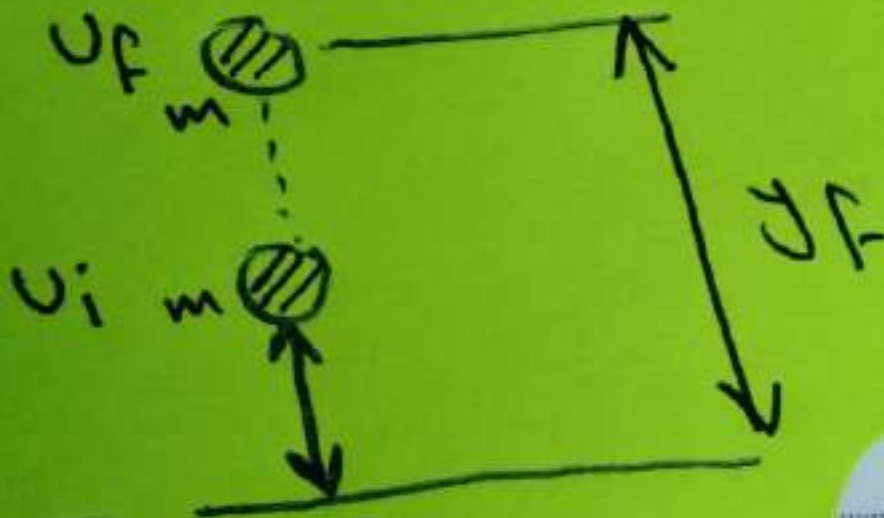
$$W = \Delta K$$

Relation between  $w$   
and P.E :

$$w = -\Delta U$$

$$= -(U_f - U_i)$$

$$= -(mgy_f - mgy_i)$$



• The change in the potential energy is  $\Delta U = mgy_f - mgy_i$

→ lose some of U work  
ect → gained some of U

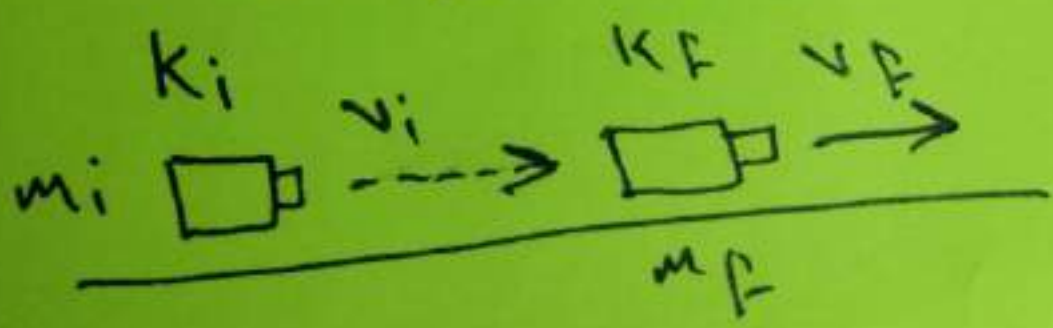
≡  $K \rightarrow J$ .

velocity

Relation ship between  
work and K.E :

Work

$$W = +\Delta K$$
$$= +(K_f - K_i)$$
$$= +\left(\frac{1}{2}mv_f^2 - \frac{1}{2}mv_i^2\right)$$



\* work mechanical [Energy theory].

$$E = k.E + p.E$$

نظام محفوظ  
نظام غير محفوظ

① Conservation system :

- No energy loss.
- No friction احتكاك

This gives that  $E = \text{constant} \rightarrow \text{conserved}$

$$\Rightarrow \Delta E = \text{Zero}$$

\* we know that:

$$w = -\Delta U = +\Delta K$$

$$-(U_2 - U_1) = (K_2 - K_1)$$

$$-U_2 + U_1 = K_2 - K_1$$

$$K_1 + U_1 = K_2 + U_2$$

$$E_1 = E_2$$

$$\Delta E = 0$$

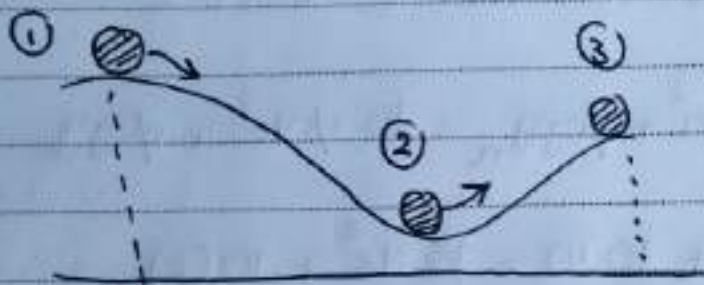
② non-conservation motion!

نظام غير محفوظ

- there is Energy loss
- Energy is not conserved.

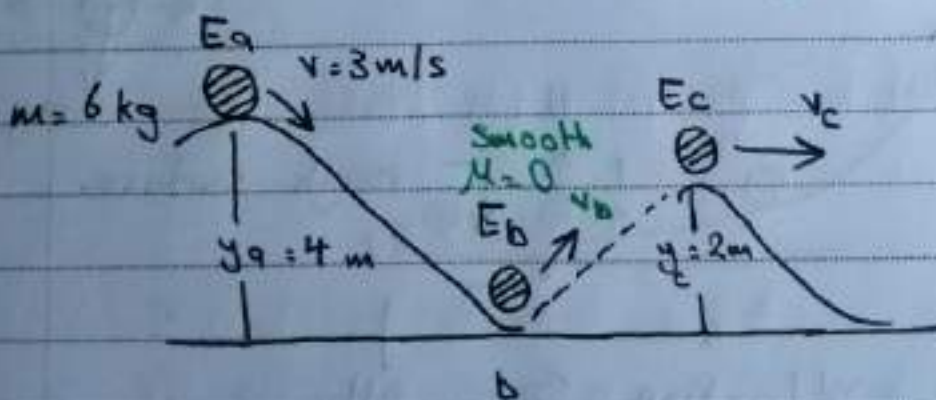
$$E_i \neq E_f \quad \Delta E \neq 0$$

- Ex: Friction.



\* In the figure,  $E$  is conserved and it change from  $K.E$  to  $P.E$  and  $U.a^2$

● Conservation law of energy:



$$E_a = E_b = E_c = \dots \quad K_a + U_a = K_b + U_b$$

$$\frac{1}{2} m v_a^2 + m g y_a = \frac{1}{2} m v_b^2 + m g y_b$$

Ex: In the figure a 6 kg object starts its motion at point a, with  $v = 3 \text{ m/s}$  moving to b then c, find its velocity at point c?

$$E_a = E_b = E_c$$

$$E_a = E_c$$

$$K_a + U_a = K_c + U_c$$

~~$$\frac{1}{2} m v^2$$~~

$$\frac{1}{2} m v_a^2 + m g y_a = \frac{1}{2} m v_c^2 + m g y_c$$

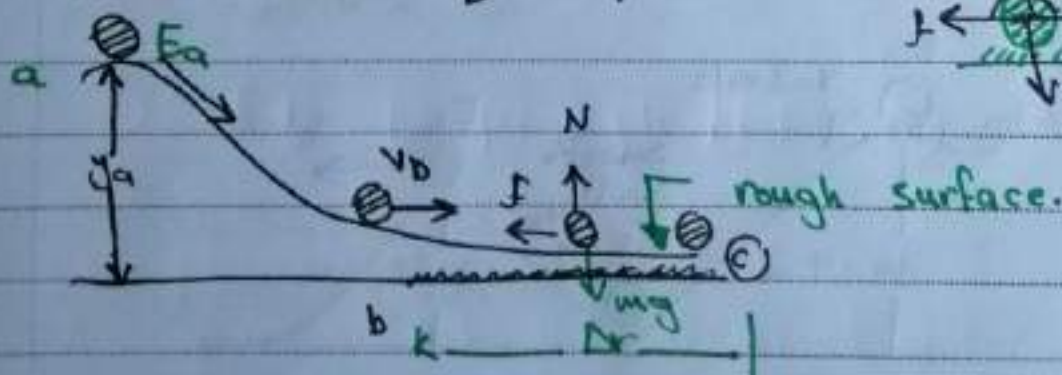
$$= \frac{1}{2} (3)^2 + 10(4) = \frac{1}{2} v_c^2 + 10(2)$$

$$4.5 + 40 = \frac{1}{2} v_c^2 + 20$$

$$24.5 \times \frac{v_c^2}{2} \quad v_c = \sqrt{49} = 7 \text{ m/s}$$

• Non-conservative system:

there is friction  $\Rightarrow \Delta E \neq 0$



$$E_f - E_i = W_{\text{friction}} \quad \leftarrow \quad \text{at } h_i$$

$$W_{\text{friction}} = |\vec{F}| \cdot |\Delta \vec{r}| \cdot \cos \theta = 180^\circ$$

$$= \mu \cdot N \cdot \Delta r \cdot -1$$

$$W_{\text{friction}} = -\mu \cdot N \cdot \Delta r$$

6

→ Power :

power : معدل إنجاز العمل / معدل القوة

$$\text{Power} = \frac{\text{work}}{\text{time}} = \frac{W}{t} = \frac{E}{t}$$

→ كمية الطاقة التي تفعلها في وحدة الزمن

$$P = \frac{\Delta W}{\Delta t} \quad \text{--- ①}$$

←  $P_{\text{avg}}$  : متوسط القوة

$P_{\text{avg}}$ : quantity of work  $\Delta W$  is done during a time  $\Delta t$ . the average work done per unit time or average power is defined to be:  $P_{\text{avg}} = \frac{\Delta W}{\Delta t}$

\*\* \* فيزياء القوة الكهربائية : القوة الكهربائية :

$$P_{\text{inst.}} = \lim_{\Delta t \rightarrow 0} \frac{\Delta W}{\Delta t} = |\vec{F}| |\vec{v}| \cos \theta$$

$$[P] = \text{J/s} = \text{watt} = \text{W} \quad \rightarrow \vec{v}$$

Kw / horse power

$$1 \text{ hp} = 746 = 0.746 \text{ Kw}$$


$$1 \text{ hp} = 3/4 \text{ Kw}$$



\* إذا كانت القوة ثابتة مع الزمن \*

$$P = \frac{W}{t} = \frac{\text{force} \cdot \text{displacement}}{t}$$

$$\therefore P = \text{force} \cdot \frac{\text{displacement}}{t} = \text{Force} \cdot \text{velocity}$$

$$P = \text{force} \cdot \text{velocity} = \vec{F} \cdot \vec{v} = F \cdot v \cdot \cos\theta$$


Examples:

If a pump lifts water of mass  $m$  from a depth  $h$  in time  $\Delta t$  then the power of the motor is given by:

$$P = W / \Delta t \quad \text{--- (1)}$$

$$W = mgh \quad \text{--- (2)}$$

$$\text{2 and 1} \Rightarrow P = mgh / \Delta t \quad \text{--- (3)}$$

Example:

A pump is used to lift 500 kg of water from a depth of 80 m in 10s. Calculate the power of the pump?  $m = 500 \text{ kg}$   $h = 80 \text{ m}$   $t = 10 \text{ s}$

$$W = mgh = 4 \times 10^5$$

$$P = \frac{W}{t} = 4 \times 10^4 \text{ watt} = 40 \text{ Kw.}$$

Example:

A 60 kg jogger runs up a long flight of stairs in 4 s. The vertical height of the stairs is 4.5 m. (a) Estimate the jogger's power output in watts and horse power. (b) How much energy did this require?

Sol.

①

$$W = mgh = 60(10)(4.5) = 2700 \text{ J}$$

①.9

$$P = W/\Delta t = \frac{2700}{4} = 675 \text{ watt} = 0.91 \text{ hp}$$

$$\text{② } P = \frac{E}{t} \quad E = 675(4) = 2700 \text{ J} //$$

Example:

A 700 N marine in basic training climbs a 10 vertical rope a constant speed of 8 s. what is his power?

$$v = d/t = 10/8 = 1.25 \text{ m/s}$$

$$P = F \cdot v \cdot \cos\theta = 1.25(700)(1) = 875 \text{ W}$$

# Chapter 6

No \_\_\_\_\_

## Ch 13 : Non viscous Fluids :

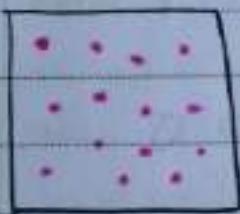
- **Fluid** is a substance that flows.

Fluid  $\left\{ \begin{array}{l} \text{liquid} \\ \text{gas} \end{array} \right.$

المادة اللينة لا يمكن أن تلتصق مع الجدران.

- **Gases** are compressible, the volume of a gas is easily increased or decreased.

قابل للانضغاط لأن حجم الغاز يأخذ حجم الوعاء الموجود فيه.



container

- **Liquid** are nearly incompressible, the molecules are packed closely, yet they can move around.



لا يمكن ضغط السائل

**Density:** the mass density is the ratio of mass to volume:

$$\rho = \frac{m}{V}$$

$$\rho = \text{kg/m}^3$$

← الكثافة مقياس يقيس الحرارة والحجم

### 13.2 : Pressure

القوة المؤثرة على وحدة المساحة

$$P = \frac{\text{Force } (F_n)}{\text{area } (A)}$$

A fluid in a container presses with an outward force against the walls of that container.

\* The pressure is defined as the ratio of the force **(to)** the area on which the force is exerted. ↪ مثال

• The SI units of pressure are  $\text{N/m}^2$

$$1 \text{ Pa} = 1 \text{ N/m}^2$$

$$1 \text{ atm} = 101.300 \text{ Pa} = 101.3 \text{ kPa}$$

$$760 \text{ mm Hg} = 1 \text{ atm}$$

$$1 \text{ atm} = 760 \text{ torr}$$

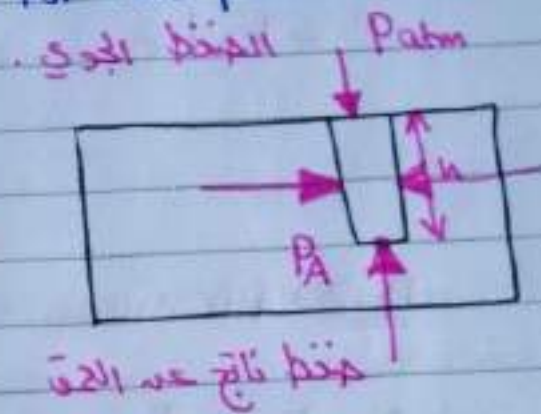
$$1 \text{ mmHg} = 1 \text{ torr}$$

### 13.3 pressure in liquids:

The force of gravity (the weight of the liquid) is responsible for the pressure in the liquid.

$$P = h\rho g + P_{atm}$$

pressure caused by liquid.      atmospheric pressure.



### Example:

The diagram shows 2 fishes in water. The density of the water is  $1025 \text{ kg/m}^3$ . The surface area of fish A is  $300 \text{ cm}^2$  and the surface area of fish B is  $2000 \text{ cm}^2$ . Find:

- The pressure exerted by water on fish A.
- The pressure " " " " B.
- The force " by the water on fish A.
- " " " " " " B.

100000 Pa  
 $\vec{P} \leftarrow \vec{P}$

Sol.

$$(a) P_a = h \rho g = 2(10)(1025) = 20500 \text{ Pa}$$

$$(b) P_b = h \rho g = 2(10)(1025) = 20500 \text{ Pa}$$

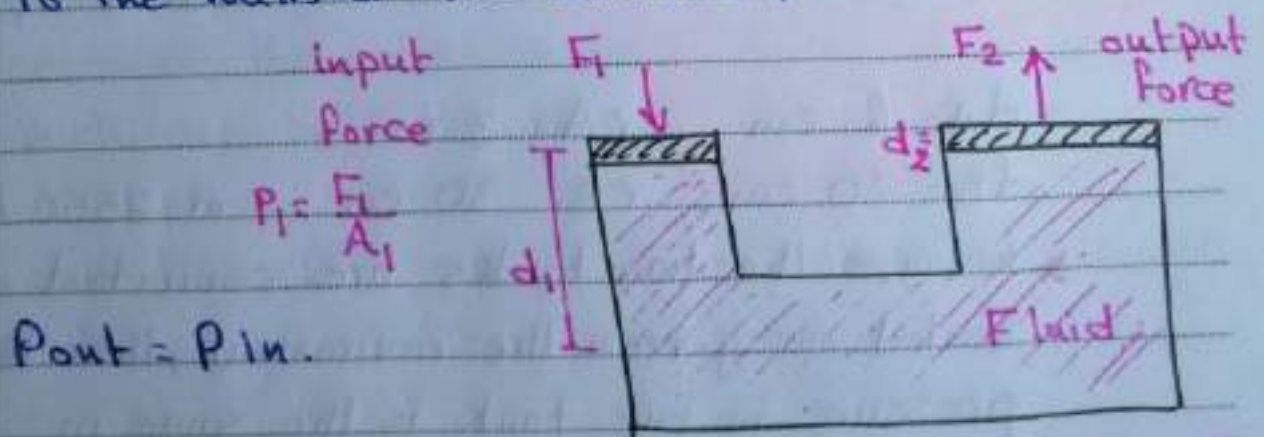
العلاقة بين الضغط والحجم والارتفاع على كثافة السائل والعمق.

$$(c) F = PA = 20500(0.03) = 615 \text{ N}$$

$$(d) F = PA = 20500(0.2) = 4100 \text{ N}$$

### 13.4: Pascal's principle:

In a fluid at rest in a closed container, a pressure change in one part is transmitted without loss to every portion of the fluid and to the walls of the container,



multiplication  
of force.

$$F_2 = \frac{A_2}{A_1} F_1$$

$$P_2 = \frac{F_2}{A_2}$$

$$P_{out} = P_{in}$$

$$\frac{F_{out}}{A_{out}} = \frac{F_{in}}{A_{in}} \quad \text{OR} \quad \boxed{\frac{F_{out}}{F_{in}}} = \frac{A_{out}}{A_{in}}$$

the mechanical advantage  
of hydraulic lift.

### Example:

A system of two tanks are connected by a skinny pipe and the system is sealed from the outside. Air is pumped into tank "A" on the left. This increases the pressure at opening "A". A hydraulic fluid is moved into tank "B" and pressure up on opening "B".

If a 2550 kg car is to be lifted by the cylinder at opening "B" then what pressure and force that must be exerted at opening "A"?

$$d_A = 6 \text{ cm} \quad r_A = 3 \text{ cm}$$

$$d_B = 60 \text{ cm} \quad r_B = 30 \text{ cm} \quad m = 2550 \text{ kg}$$

→ because the two tanks are connected and sealed away from the environment, then the pressure in one tank is the same in

→ Use pascals principle to find  $F_A$ .

$$P_A = P_B$$

$$\frac{F_A}{A_A} = \frac{F_B}{A_B}$$

$$\frac{F_A}{\pi(r_A)^2} = \frac{F_B}{\pi(r_B)^2}$$

$$\frac{F_A}{\pi(r_A)^2} = \frac{F_B W_B}{\pi(r_B)^2}$$

$$\frac{F_A}{\pi(r_A)^2} = \frac{m_b g}{\pi(r_B)^2}$$

$$\frac{F_A}{\pi(0.03m)^2} = \frac{2550(9.8) \frac{m}{s^2}}{\pi(0.30m)^2}$$

$$F_A = 249.9 N$$

### 13.5 Blood Pressure :

- Blood pressure is measured by pressurizing a cuff around a patient's arm.

- The cuff squeezes the artery shut. when the cuff pressure drops below the systolic (max) blood pressure, the artery pushes blood through in pulses, which can be heard through a stethoscope

- when the cuff pressure drops below the diastolic pressure, blood flows smoothly.



$$F_A = 249.9 \text{ N}$$

له قرائن > سفلية  
علوية

(max min)  
الكبيبي (120 - 80)

حتى أفيد المنفذ بطريقة  
محددة منه على ذراع اليد القريبة  
وهو مستوى القلب لروية البنح  
في الشريان.

pressure drops below the diastolic  
flows smoothly.

→ The patient's arm is held at about the same height as her heart?

The hydrostatic pressure of a fluid varies with height. Although flowing blood is not in hydrostatic equilibrium, it is still true that blood pressure increases with the distance below the heart and decreases above it.

Because the upper arm when held beside the body is at the same height as the heart, the pressure here is the same as the pressure at the heart. If the patient held her arm straight up, the pressure cuff would be a distance  $d \approx 25$  cm above her heart and the pressure would be less than the pressure at the heart by  $\Delta p = \rho_{\text{blood}} g d \approx 20$  mmHg.

\* الضغط الذي خارج يتغير مع تغير الارتفاع  
بالتي الضغط يتغير حسب موقع القياس  
أما إذا كان نفس مستوى القلب  
\* بما أن الدم في حالة حركة دائمة فإنه لا يكاد في حالة انزاح تلك عند قياس الضغط بالقرب من القلب نقول أنه قريباً تقريباً

## 13.6 Buoyancy:

الطفو

وهي عبارة عن قوة يرفعها السائل  
على سطح الجسم.

is the upward force of a liquid.

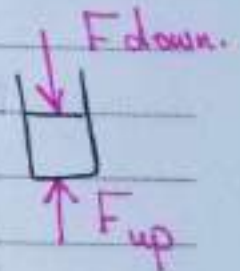
→ The pressure in a liquid increases with depth, so the pressure in a liquid-filled cylinder is greater at the bottom than at the top.

The pressure exerts a net upward force on a submerged cylinder of:

$$F_{net} = F_{up} - F_{down}$$

$$= F_B$$

$$** F_B = W$$



← اتجاه قوة الرفع عمودية للأعلى ← تسبب في دفع  
الجسم الجسم للأعلى ← يغير توازنه مع الجسم أو السائل  
والتأثير.

← يزداد الارتفاع كلما زاد عمق السائل.

∴ يتولد عندي خطين: ① عند قاع البحر أو السائل  
أعلى من خط ال Top.

② عند السطح أو أقل من الخط عند القاع  
وهو في الأسفل < فهو في الأعلى.

عند الاتزان: قوة الرفع = الوزن.

### 13.7 : Archimedes principle:

states that the upward buoyant force that is exerted on a body immersed in a fluid, whether fully or partially submerged, is equal to the weight of the fluid that the body displaces.

$$F_B = \rho_F V_P g$$

Fluid density.      Fluid volume.

$\rho = \frac{m}{V}$        $m = \rho V$

$$F_B \Rightarrow N$$

#### Example ①

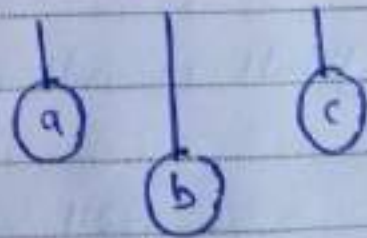
Blocks a, b and c are all the same size.  
Which is the correct order of the scale readings?

a) 40 g

b) 40 g

c) 50 g

$$c > a = b$$



\* هل يرتبط الالف بالارتفاع ؟ لا

Ex 2:

A piece of metal weighs 9.25g in air, and 8.2g in water, and 8.36g when immersed in gasoline?

(a) What is the density of the metal?

$$9.25 - 8.20 = \underline{1.05g}$$

$$\rho = \frac{m}{V} \quad V = \frac{1.05}{1} = 1.05 \text{ cm}^3$$

$$\text{the density} = \frac{9.25}{1.05} = 8.81 \text{ g/cm}^3$$

H.w

(b) What is the density of the gasoline?

$$m \rightarrow 9.25 - 8.36 = 0.89$$

$$\text{the density} = \frac{0.89}{1.05} = 0.85 \text{ g/cm}^3$$

H.w: An object weighs 36g in air,  $V = 8 \text{ cm}^3$ .  
What will be its apparent weight when immersed in water?

$$W = 36 \text{ in air} \quad V = 8 \text{ cm}^3 \quad \rho = 1 \text{ g/cm}^3$$

$$36 - x = 8$$

$$x = 28 \text{ g}$$

10

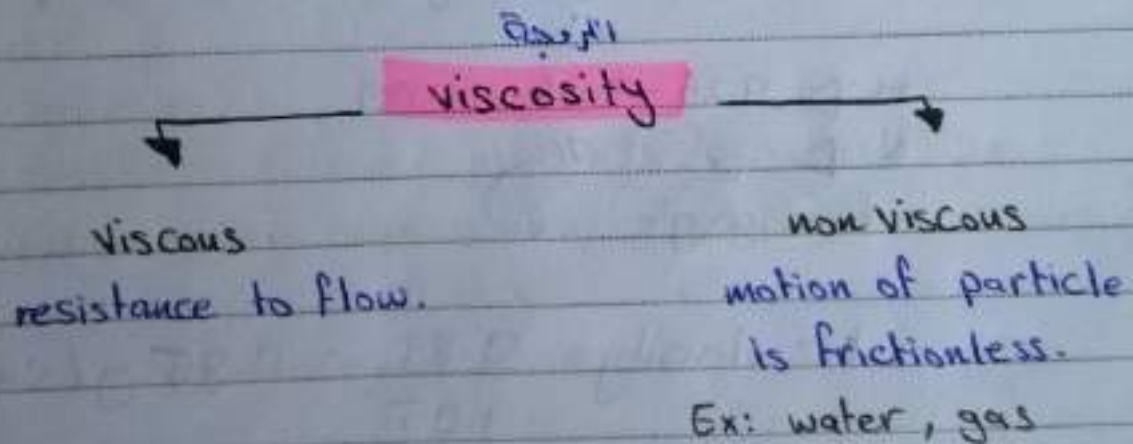
# Chapter 7

## Ch 14 Fluids and motion:

- The Fluid is  $\left\{ \begin{array}{l} \text{Compressible} \rightarrow \text{gases.} \\ \text{Incompressible} \rightarrow \text{liquids.} \end{array} \right.$

$\rightarrow$  The flow is steady, the fluid velocity at each point in the fluid is constant  $\rightarrow$  is called **laminar flow**.

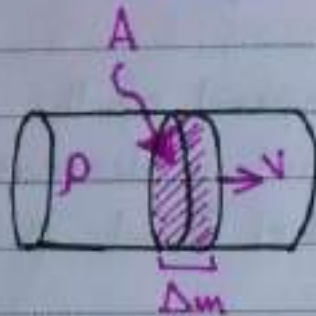
$\rightarrow$  The flow is unsteady, the fluid velocity changes with time  $\rightarrow$  is called **turbulent flow**.



\* Gases have very low viscosity and even many liquids are well approximated as being non viscous.

## 14.2 Fluid mass flow rate $Q$

is the mass of a fluid which passes per unit of time,  $(\text{kg/sec})$



$$Q = \frac{\Delta m}{\Delta t} = \rho \cdot A \cdot v$$

$\rho$ : Fluid density  
 $A$ : area  
 $v$ : flow velocity speed

## 14.3 : The Equation of continuity:

The volume of an incompressible fluid entering one part of a tube or pipe must be matched by an equal volume leaving downstream.

الكمية الداخلة = الكمية الخارجة  
 $\rho_1 A_1 v_1 = \rho_2 A_2 v_2$

inlet:  $Q_1 = \rho_1 A_1 v_1$       outlet:  $Q_2 = \rho_2 A_2 v_2$

$$Q_1 = Q_2$$

$$\therefore A_1 v_1 = A_2 v_2 \Rightarrow \text{السرعة تتناسب عكسياً مع المساحة}$$

السرعة تتناسب عكسياً مع المساحة

\* Flow is faster in narrower parts of a tube, slower in wider parts.

#### 14.4 Bernoulli's Equation: . زيادة السرعة $\rightarrow$

increase in the speed of the fluid occurs simultaneously with a decrease in pressure or decrease in the fluid's potential energy.

OR

In a horizontal pipe, the highest fluid pressure is in the section where the flow speed is the lowest, and the lowest pressure is at the section where the flow speed is the sp biggest.

. في ارتفاع الارتفاع  $\rightarrow$  انخفاض السرعة  
زيادة السرعة في السطح  $\rightarrow$  مثال من ارتفاع  $\rightarrow$  انخفاض السرعة

. الكتلة في الداخل = الكتلة في الخارج

$$P_1 + \frac{1}{2} \rho v_1^2 + \rho g h_1 = P_2 + \frac{1}{2} \rho v_2^2 + \rho g h_2$$

14.5

$\rightarrow$  mass conservation principle  $\Rightarrow$  the equation of continuity.

$\rightarrow$  Energy conservation principle  $\Rightarrow$  Bernoulli's Equation.



$$P_1 > P_2$$

$$A_1 > A_2$$

$$v_1 < v_2$$

$$\rho_1 A_1 v_1 = \rho_2 A_2 v_2$$

إذا كان المقطع أكبر

فإن السرعة تكون أصغر

القانون

تكون السرعة أكبر

the speed of the fluid increases  
continuously with a decrease in pressure  
or a decrease in the fluid's potential energy.

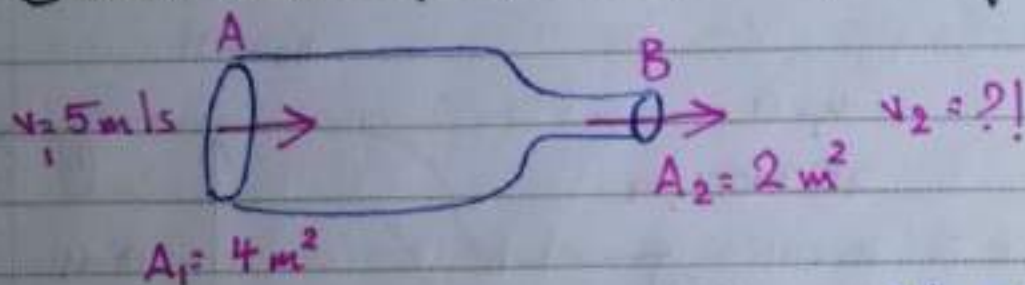
OR

In a horizontal pipe, the highest fluid pressure  
is in the section where the flow speed

### Example ① :

Water flows through a horizontal pipe with a cross-sectional area of  $4\text{m}^2$  at a speed of  $5\text{ m/s}$  with a pressure of  $300000\text{ Pa}$  at point A. At point B, the cross-sectional area is  $2\text{m}^2$ .

① what is the speed of water at point B?



$$A \downarrow \Rightarrow v \uparrow$$

$$A_1 v_1 = A_2 v_2$$

$$4(5) = 2v_2$$

$$\frac{20}{2} = v_2$$

$$v_2 = 10\text{ m/s}$$

② Calculate the pressure at point B?

$$A_1 = 4\text{ m}^2 \quad P_1 = 300000\text{ Pa}$$

$$A \downarrow \quad v \uparrow$$

$$P = \frac{F}{A}$$

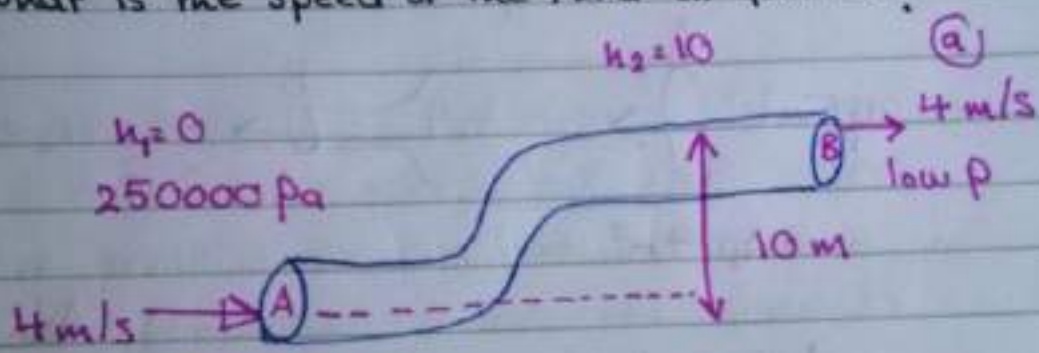
$$P_1 + \rho g h_1 + \frac{1}{2} \rho v_1^2 = P_2 + \rho g h_2 + \frac{1}{2} \rho v_2^2$$
$$300000 + \frac{1}{2} (1000)(5)^2 = P_2 + \frac{1}{2} (1000)(10)^2$$

$$P_2 = 262,500\text{ Pa}$$

Example ②:

water flows through a circular ~~radius~~ pipe with a constant radius of 10 cm. The speed and pressure at point A is 4 m/s and 250,000 Pa respectively.

① What is the speed of the fluid at point B?



$$P_1 + \cancel{\rho gh_1} + \frac{1}{2} \cancel{\rho v_1^2} = P_2 + \rho gh_2 + \frac{1}{2} \rho v_2^2$$

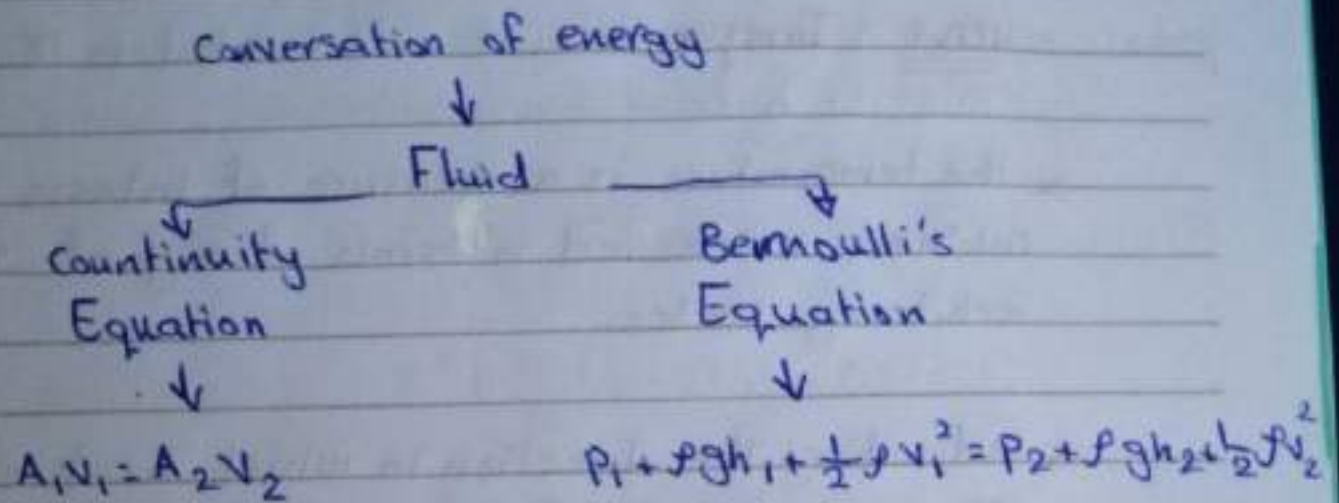
$$250000 = P_2 + 1000 (9.8) (10)$$

$$250000 = P_2 + 98000$$

$$P_2 = 152000 \text{ Pa} \quad \text{②}$$

② what is the pressure at point B which is 10 m higher than point A? ↑

## 14.5: Energy Conservation:



H.W.:

Water circulates throughout a house in a hot water heating system. If the water is pumped at a speed of 0.50 m/s through a 4 cm diameter pipe in the basement under a pressure of 3 atm. What will be the flow speed and pressure in a 2.6 cm diameter pipe on the second floor 5 m above? Assume the pipes do not divide into branches.

$v_2 = \frac{A_1 v_1}{A_2} = \frac{v_1 (\pi r_1^2)}{\pi (r_2)^2} = 1.2 \text{ m/s}$

$$P_1 + \rho g h_1 + \frac{1}{2} \rho v_1^2 = P_2 + \rho g h_2 + \frac{1}{2} \rho v_2^2$$

$$P_2 = P_1 + \rho g (h_1 - h_2) + \frac{1}{2} \rho (v_1^2 - v_2^2)$$
$$= 2.5 \times 10^5 \text{ N/m}^2$$

# Chapter 8

No. \_\_\_\_\_

## Ch 15: Temperature

### 15.1 Temperature:

→ The temperature is a measure of hotness or coldness expressed in terms of any of several arbitrary scales.

→ Indicating the direction in which heat energy will spontaneously flow.

← حياض مسوية أو برودة.

\*\* Temperature is not heat and heat is one of energy forms.

← انتقال أو انتقال الطاقة.

### 15.2 Thermometers:

A thermometer is a device/instrument that measures temperature.

Thermometer work based on → physical phenomenon

بعض المواد - most materials exhibit a change in size with changes in temperature.

تغير شكلها

تغير حرارتها

- Common thermometer is used today are liquid in glass type and bimetallic strip

### 15.3 Temperature Scales:

There are three temperature scales in use today:  
Celsius, Fahrenheit and Kelvin.  $\overset{\circ}{=} 15.6$

$$C \rightarrow F \quad F^{\circ} = \frac{9}{5} C^{\circ} + 32$$

$$K \rightarrow F \quad F^{\circ} = \frac{9}{5} (K - 273) + 32$$

$$F \rightarrow C \quad C^{\circ} = \frac{5}{9} (F^{\circ} - 32)$$

$$C \rightarrow K \quad K = C^{\circ} + 273$$

$$K \rightarrow C \quad C^{\circ} = K - 273$$

$$F \rightarrow K \quad K = \frac{5}{9} (F^{\circ} - 32) + 273$$

Example (1):

$$98.6^{\circ} F \rightarrow C^{\circ}$$

$$C^{\circ} = \frac{5}{9} (98.6 - 32) = 37^{\circ}$$

Example (2):  $10^{\circ} C \rightarrow F^{\circ}$

$$F^{\circ} = \frac{9}{5} (10) + 32 = 18 + 32 = 50 F^{\circ}$$

Example (3):

The boiling temperature of liquid oxygen at normal pressure at  $-182.96^{\circ}\text{C}$ . what is the value in K?

$$K = C + 273.15$$

$$K = 90.19 \text{ K.}$$

Example (4):

$$C = 25^{\circ}\text{C} \rightarrow K$$

$$K = C^{\circ} + 273.15 = 298.15$$

Ex (5)

$$K \rightarrow F^{\circ}$$

$$K = 293$$

$$F^{\circ} = \frac{9}{5} (K - 273) + 32 = 68^{\circ}\text{F}$$

Ex (6)

$$F = 98.6^{\circ}\text{F} \rightarrow K$$

$$K = \frac{5}{9} (F - 32) + 273 = 310.15 \text{ K.}$$

# Chapter 9

ch 30: Nuclear physics

Introduction: Atomic structure.

The atomic nucleus is a very small dense object. Its size is  $\approx 1 \text{ fm}$  ( $1 \text{ fm} = 10^{-15} \text{ m}$ ),  $10^{-4} \times$  the size of an atom. The nucleus is made up from two kinds of nucleons: **protons** and **neutrons**. The proton has a positive electrical charge equal in magnitude the electrons charge and a mass about 1840 times the mass of  $e^-$ . The neutron (discovered by James Chadwick in 1932) is a neutral particle slightly heavier than the p.

A nucleus is specified by **atomic number  $Z$**  (number of protons) and its **mass number  $A$**  (number of neutrons and protons  $A = N + Z$ ). The **number of neutrons** is then  $N = A - Z$ .

(1)



Example :

The  $^{238}_{92}\text{U}$  or  $^{238}\text{U}$  has 238 nucleons, of which 92 are protons and  $238 - 92 = 146$  n.

Nuclides which have the same atomic number but different number of neutrons are called isotopes such as Deuterium  $^2_1\text{H}$  and tritium  $^3_1\text{H}$ , isotopes of the hydrogen nuclide  $^1_1\text{H}$ .

### 30.1 Radioactivity:

In 1896 Henri Becquerel noted that uranium compounds produce invisible radiations that can penetrate opaque containers and expose photographic emulsion. Many other radionuclides were subsequently found.

The radioactivity or radioactive decay; is a spontaneous and random process in which three kinds of particles can be emitted:

- **Gamma decay:** a photon of high energy is emitted, (greater than those of x-rays)  
mass less

(2)

- Alpha decay: emission of the particle  $\alpha$   ${}^4_2\text{He}$  (process followed with a nuclear transmutation).

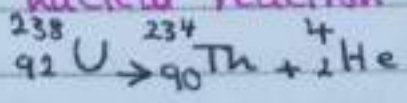
- Beta decay: an electron  $\beta^-$  or positron  $\beta^+$  can be emitted with a neutrino.

معرفة  
تفسير

### Radioactivity

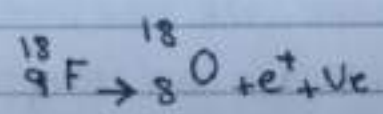
### nuclear reaction

Alpha



A transmutation of the uranium-238 into Thorium-234

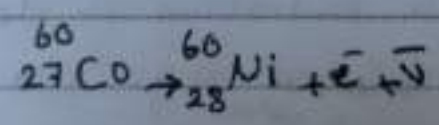
Beta ( $\beta^+$ )



Transmutation of a proton into neutron

Transmutation of the fluorine-18 into oxygen

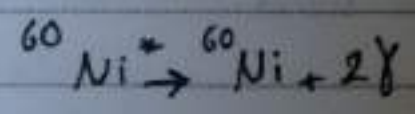
Beta ( $\beta^-$ )



Transmutation of a neutron into proton.

Transmutation of the cobalt-60 into Ni-60.

Gamma



Unstable Nickel emits  $\gamma$ -ray, the nucleus remains the same.

\*\* The radioactive decay of nuclei produces several types of ionizing radiation with several mega electron volts per particle.

It was found that when these radiations pass through the body, they can cause biological hazardous such as cell damage, skin burns and cancer.

• Ionizing radiation have the ability to penetrate matter. لديه القدرة على اختراق المواد

- أقل طاقة Alpha particles are stopped by a sheet of paper.
- Beta particles can be stopped with a thin foil of Tin or aluminum.

• الأكثر خطراً Gamma radiation is dampened when it penetrates matter. Gamma rays can be stopped from 4 meters of <sup>volt</sup> lead. Tungsten and tungsten alloys can stop Gamma radiation with much less mass than lead.

- Half-life:

اس وقت

A nuclear decay is a random process, we cannot predict in any way when a specific nucleus will decay. Nevertheless, the process can be characterized by a specific parameter: the half life

- If at time  $t=0$  there are  $N_0$  nuclei, then on a half time later,  $T$ , an average of  $\frac{N_0}{2}$  will remain.
- At  $t=2T$ , when two half life lives have elapsed, half of these, or  $N_0/4$  nuclei will be left; At  $t=3T$ ,  $N_0/8$  will be left, and so on.
- Depending on the nuclide, the half-life may vary from a small fraction of second to billions of years.

when the elapsed time is not an integer multiple of the half-life, we can find the number of nuclei remaining as follows:

The change of the number of nuclei  $\Delta N$  in a small time  $\Delta t$  is proportional to  $N$  and  $\Delta t$ :

$$\Delta N = -\lambda N \Delta t$$

half life  $\leftarrow$

→ The last equation implies that if at  $t=0$  there are  $N_0$  nuclei, later at time  $t$  the number of remaining nuclei is given by the equation:

$$N = N_0 e^{-\lambda t}$$

- This equation is called the exponential decay formula.
- $\lambda$  is the constant decay.
- In terms of fraction of radioactive nuclei remaining after time  $t$  we get:  $\frac{N}{N_0} = e^{-\lambda t}$
- A graphical representation of  $\frac{N}{N_0}$  is shown in fig.

we can easily show that the decay constant is related to the half-life time by:

$$\lambda T = \ln(2) \quad \text{or} \quad \lambda T = 0.693$$

$$\ln 2 = 0.693$$

Examples:

①

Plutonium decays with a half-life of 24000 years. If plutonium is stored for 72000 years, the fraction of it that remains is

(a)  $\frac{1}{2}$

(b)  $\frac{1}{3}$

(c)  $\frac{1}{4}$

(d)  $\frac{1}{8}$

Sol.: The half-life of plutonium is given to be 24000 years. It is stored for a period of 72000 years. So, the number of half-life periods =  $72000 / 24000 = 3$

The fraction that remains is given by  $\frac{1}{2} = \frac{1}{8}$

②

The decay constant ( $\lambda$ ) and the half-life ( $T$ ) of a radioactive isotope are related as:

(a)  $\lambda = \frac{1}{\log_e 2T}$

(b)  $\lambda = \frac{1}{\log_e 2}$

(c)  $\lambda = \frac{2}{T}$

(d)  $\lambda = \log_e 2 / T$

Sol.: The relation between the half-life and the decay constant is given by half-life

$$T = 0.693 / \lambda$$

$$\Rightarrow \lambda = \log_e 2 / T$$

⑦

3

An isotope is:

- (a) an atom with a different number of  $e^-$ .
- (b) an atom with a different number of proton.
- (c) an atom with a different number of neutrons
- (d) an atom with a different number of p & n.

4

Cobalt has an atomic mass of 59 and atomic number of 27. what does this information reveal about most cobalt atoms?

- (a) They contain more neutrons than protons.
- (b) // naturally have a net negative charge.
- (c) // attract protons more strongly than  $e^-$ .
- (d) // form ions with a charge of +27 in compounds.

5

The atomic mass is:

- (a) the number of  $e^-$  in an atom.
- (b) // // " p // // "
- (c) // // " n // // "
- (d) // // " p+n // // "

8

6)

الرمز الصحيح للذرة التي

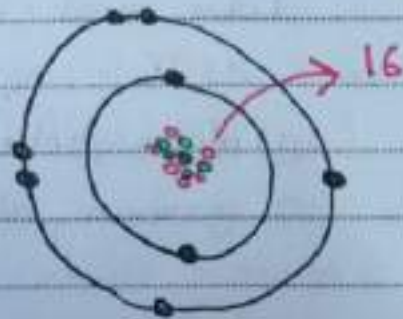
which is the correct symbol for the atom with 42 protons and 49 neutrons?

- a.  ${}^{49}_{42}\text{In}$     b.  ${}^{91}_{42}\text{Mo}$     c.  ${}^{91}_{49}\text{Mo}$     d.  ${}^{91}_{42}\text{In}$

7)

which is the correct symbol for the following atom?

- a.  ${}^{24}_{16}\text{O}$     b.  ${}^{16}_{24}\text{Cr}$   
 c.  ${}^{24}_{16}\text{S}$     d.  ${}^{16}_{8}\text{O}$



8)

مما

The half-life of an isotope is the time required for half the nuclei in a sample to:

تبقى half life

- a. undergo radioactive decay. ✓  
 b. undergo nuclear fission.  
 c. " " fusion. ]  
 d. react chemically. ]

9



(9)

which type of nuclear radiation can be blocked by a piece of paper?

- a. alpha      b. beta      c. gamma      d. none can be blocked by paper

(10)

which of the following lists ranks nuclear radiation from most massive (size wise) to least massive?

- a. alpha, beta, gamma.      b. beta, gamma, alpha.  
c. gamma, alpha, beta.      d. gamma, beta, alpha

(11)

The half-life of decay of strontium-90 is 28.8 years. A milk sample is found to contain 10.3 ppm strontium-90. How many years would pass before the strontium-90 concentration would drop to 1.0 ppm? particle per million

- a. 92.3      b. 0.112      c. 186      d. 96.9

Given data: - the half-life beta decay of Strontium-90 is 28.8 years.

(10)

- The initial concentration of strontium-90 is 10.3 ppm
- The final concentration of strontium-90 is 1.0 ppm

Radioactive beta decay always follows first order kinetics.

Therefore the half-life can be used to calculate the rate of reaction using the formula shown below.

$$\lambda = \frac{0.693}{t_{1/2}}$$

where,  $\lambda$  is the rate constant for the beta decay.  
 $t_{1/2}$  is the half-life of the decay.

Substitute the values in the above formula.

$$\lambda = \frac{0.693}{28.8 \text{ years}} = 0.024 \text{ years}^{-1}$$

The integrated form of a first order reaction is shown below.

$$N = N_0 e^{-\lambda t}$$

where,  $N$  is the final concentration.

$N_0$  is the initial concentration.

$\lambda$  is the rate constant.

$t$  is the time.



Substitute the known values in the above formula.

$$10.3 \text{ ppm} = 1 \text{ ppm} \times e^{-0.024 \text{ years}^{-1} \times t}$$

$$e^{-0.024 \text{ years}^{-1} \times t} = 10.3$$

$$-0.024 \text{ years}^{-1} \times t = \ln(10.3)$$

$$t = \frac{-2.332}{-0.024 \text{ years}^{-1}}$$

Therefore,  $t = 97.166$  years

Hence, the time required for the concentration of strontium-90 to decrease to 1.0 ppm is 97.166 years.

$$N(t) = N_0 \times e^{(-\lambda \times t)}$$

$$1 = 10.3 \times e^{-(0.024 \times t)}$$

$$\rightarrow \lambda = 0.024 \text{ 1/y}$$

$$= 0.24 \text{ y}^{-1}$$

$$\frac{1}{10.3} = e^{-(0.024 \times t)}$$

$$0.097 = e^{-(0.024 \times t)}$$

$$\ln 0.097 = \ln e^{-(0.024 \times t)}$$

$$\ln 0.097 = -\lambda t$$

(12)

$$-2.33 = -0.024 t$$

$$t = 97 \text{ years} \Rightarrow d$$

(12)

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The half-life of I is 0.220 years. How much of a 500.0 mg sample remains after 24 hours?

- a. 496 mg    b. 560 mg    c. 219 mg    d. 405 mg

$$T = 0.22 \quad y = 0.22 \times 365 \times 24 = 1927 \text{ h}$$

$$N_0 = 500 \text{ mg} \xrightarrow[t = 24 \text{ h}]{\quad} N = ? \text{ mg}$$
$$N = 500 \text{ mg} \times \left(\frac{1}{2}\right)^{24/1927} = 496 \text{ mg.}$$

(13)

أسأل الله لكم التوفيق 